

MEASURING STOP MIXING ANGLE AT THE LHC

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Motivation

- stops play an important role in the mechanism of radiative electroweak symmetry breaking
- CP-violating phase in stop sector can have a large impact on the Higgs sector of MSSM and play significant role in baryogenesis
- can be inaccessible at the linear collider (at least at the first stage)
 - ⇒ extract as much information as possible from LHC
 - ⇒ for what can be done at the ILC see:
Bartl ea. '95-'99, '04, Kraml '99
- here we propose a new method to determine properties of the stop sector at the LHC

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- 1 Introduction
- 2 Ratios of branching ratios
- 3 Parameter determination
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Stop sector of the MSSM

- defined by soft SUSY breaking masses for squarks \widetilde{M}_Q , \widetilde{M}_U , soft trilinear coupling A_t , $\tan \beta$ and μ parameter
- mass matrix for scalar top quarks in gauge eigenstate basis \tilde{t}_L, \tilde{t}_R

$$\mathcal{M}_{\tilde{t}}^2 = \begin{pmatrix} m_t^2 + m_{LL}^2 & m_{LR}^* m_t \\ m_{LR} m_t & m_t^2 + m_{RR}^2 \end{pmatrix}$$

with

$$m_{LL}^2 = \widetilde{M}_Q^2 + m_Z^2 \cos 2\beta \left(\frac{1}{2} - \frac{2}{3} s_W^2 \right)$$

$$m_{RR}^2 = \widetilde{M}_U^2 + \frac{2}{3} m_Z^2 \cos 2\beta s_W^2$$

$$m_{LR} = A_t - \mu^* (\cot \beta)$$

Stop sector of the MSSM

- diagonalize mass matrix with unitary matrix $U_{\tilde{t}}$

$$U_{\tilde{t}} \mathcal{M}_{\tilde{t}}^2 U_{\tilde{t}}^\dagger = \text{diag}(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2)$$

- obtain mass matrix eigenstates \tilde{t}_1 and \tilde{t}_2

$$\begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} = U_{\tilde{t}} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} = \begin{pmatrix} \cos \theta_{\tilde{t}} & \sin \theta_{\tilde{t}} e^{-i\phi_{\tilde{t}}} \\ -\sin \theta_{\tilde{t}} e^{i\phi_{\tilde{t}}} & \cos \theta_{\tilde{t}} \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

- stops interactions can be parametrized in terms of $\cos \theta_{\tilde{t}}$ and $\phi_{\tilde{t}}$

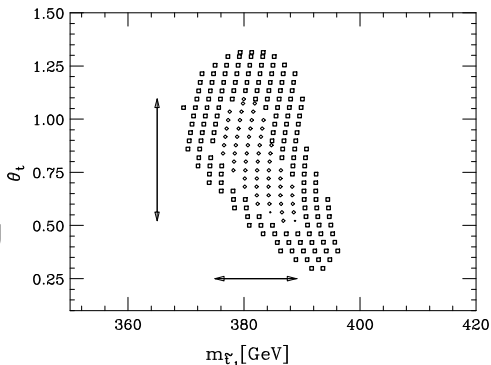
Methods to determine $\cos \theta_{\tilde{t}}$

- take stops from gluino decays
 $\tilde{g} \rightarrow t\tilde{t} \rightarrow tb\tilde{\chi}_1^+$
 $\tilde{g} \rightarrow b\tilde{b}_i \rightarrow tb\tilde{\chi}_1^+$
- combine the analysis of sbottom and stop sectors
- fit to stop mass and mixing angle gives:

$$\Delta m_{\tilde{t}_1} = 7 \text{ GeV}$$

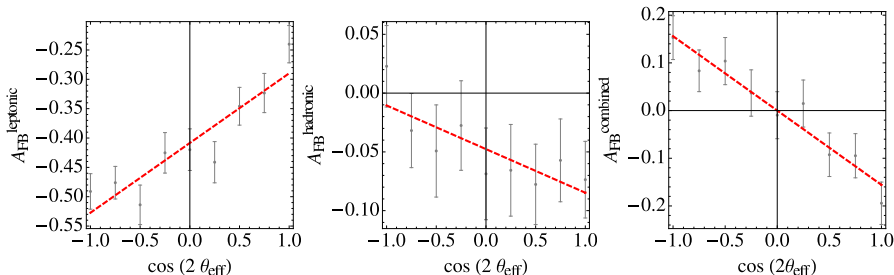
$$\Delta \theta_{\tilde{t}} = 0.29$$

Hisano, Kawagoe, Nojiri '03



Methods to determine $\cos \theta_{\tilde{t}}$

- measurement of top polarization in the decay $\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t$
- use hadronic and semileptonic top decays and forward-backward asymmetries A_{FB} of decay products
- A_{FB} have linear dependence on **effective** stop mixing angle
Perelstein, Weiler '08



Stop couplings

- consider the coupling to charged gauginos and higgsinos

$$\mathcal{L} \supset ig_2 \tilde{t}_L^* \tilde{W}^+ b_L + Y_t \tilde{t}_R^* \tilde{H}_u^+ b_L + Y_b \tilde{t}_L^* \tilde{H}_d^+ b_R + \text{h.c.}$$

- $\cos \theta_{\tilde{t}}$ gives content of \tilde{t}_L and \tilde{t}_R states in \tilde{t}_1 and \tilde{t}_2

$$\tilde{t}_L = \tilde{t}_1 \cos \theta_{\tilde{t}} - \tilde{t}_2 \sin \theta_{\tilde{t}}$$

- for mass eigenstates we have

$$\mathcal{L} \supset ig_2 \cos \theta_{\tilde{t}} \tilde{t}_1^* \tilde{W}^+ b_L - ig_2 \sin \theta_{\tilde{t}} \tilde{t}_2^* \tilde{W}^+ b_L + \dots$$

\Rightarrow for $\cos \theta_{\tilde{t}} = 0$ coupling of \tilde{t}_1^* to wino vanishes

\Rightarrow for $\cos \theta_{\tilde{t}} = 1$ coupling of \tilde{t}_1^* to wino maximal

Our method

- measuring relative strength of the coupling to charginos and neutralinos gives information on the structure of stop sector
- take light stops from a direct pair production process to avoid background from sbottoms
- absolute measurement of branching ratios difficult
 - ⇒ look at the relative number of stops decaying to different charginos and neutralinos
- depending on the realized model one can get information on stop mixing (including phase) and mass
 - ⇒ can be combined with information from other methods

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Parameter point – SPS1a'

- masses:

$$m_{\tilde{t}_1} = 366 \text{ GeV}$$

$$m_{\tilde{\chi}_1^\pm} = 184 \text{ GeV}$$

$$m_{\tilde{\chi}_1^0} = 98 \text{ GeV}$$

$$m_{\tilde{\chi}_2^0} = 184 \text{ GeV}$$

- mixing angle: $\cos \theta_{\tilde{t}} = 0.56$,
 $\phi_{\tilde{t}} = 0$

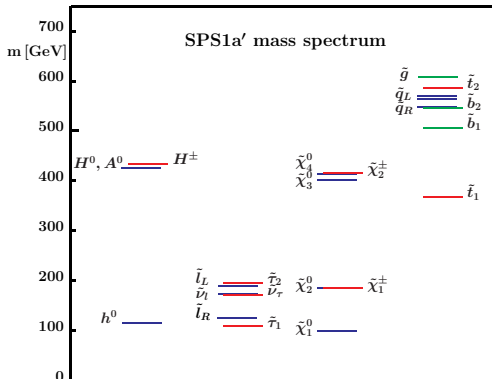
- decay modes:

$$BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^+ b) = 72\%$$

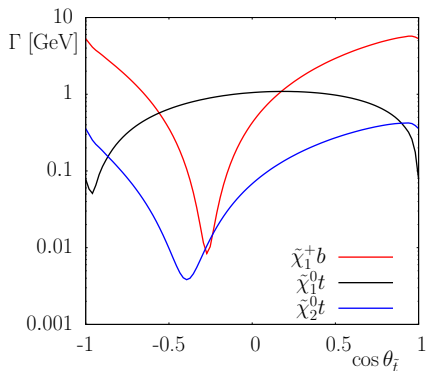
$$BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t) = 22\%$$

$$BR(\tilde{t}_1 \rightarrow \tilde{\chi}_2^0 t) = 7\%$$

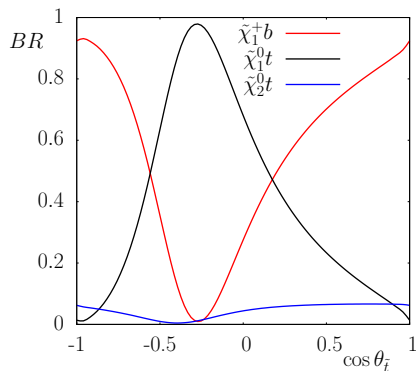
- $\sigma^{14 \text{ TeV}}(pp \rightarrow \tilde{t}_1 \tilde{t}_1^*) = 3.4 \text{ pb}$



Stop decays



widths for different decay modes
of \tilde{t}_1 as a function of $\cos \theta_{\tilde{t}}$



BRs for different decay modes
as a function of $\cos \theta_{\tilde{t}}$

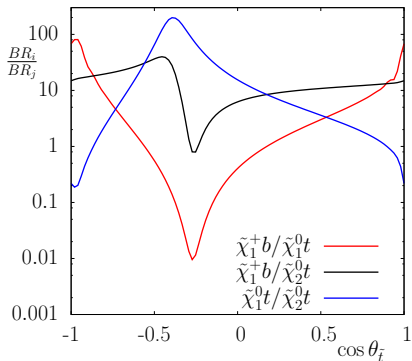
Ratios of branching ratios

- define the following quantities in \tilde{t}_1 decay modes:

$$R_{1t}^{1b} = \frac{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^+ b)}{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t)}$$

$$R_{2t}^{1b} = \frac{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^+ b)}{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_2^0 t)}$$

$$R_{2t}^{1t} = \frac{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_1^0 t)}{BR(\tilde{t}_1 \rightarrow \tilde{\chi}_2^0 t)}$$



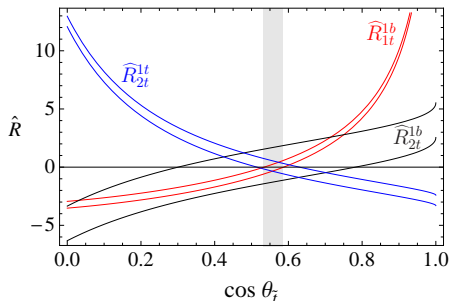
ratios of BRs for different decay modes as a function of $\cos \theta_{\tilde{t}}$

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Determination of stop mixing angle

- number of events for any two decay modes give one of the ratios R_{ij}^i
 - \Rightarrow best constraints from R_{1t}^{1b} and R_{2t}^{1t}
 - \Rightarrow no information on other decay modes required



- here ratios are normalized to their nominal values with $1-\sigma$ statistical error bands

Fit results for $\cos \theta_{\tilde{t}}$ and $m_{\tilde{t}_1}$

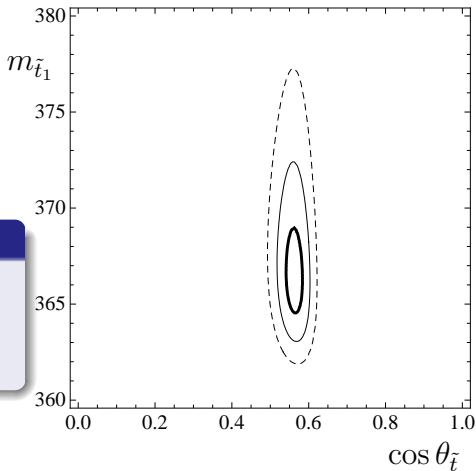
- 1000 events of stop production
- χ^2 fit to all 3 ratios
- error = statistical only

Results

$$\cos \theta_{\tilde{t}} = 0.56 \pm 0.04$$

$$\theta_{\tilde{t}} = 0.98 \pm 0.05$$

$$m_{\tilde{t}_1} = 366^{+3}_{-2} \text{ GeV}$$



SM Backgrounds

- Standard Model background:

$$t\bar{t} \rightarrow 4j\ 2b, \quad 2j\ 2b\ \ell + E_{\text{miss}}, \quad 2b\ 2\ell + E_{\text{miss}}$$

- cuts proposed by **Perelstein, Weiler '08**

- ⇒ large missing transverse energy $E_{\text{miss}} > 125\text{ GeV}$
- ⇒ semileptonic top veto (using neutrino momentum reconstruction)
- ⇒ hadronic top reconstruction to eliminate W +jets background
- ⇒ angular and separation cuts

SUSY Backgrounds

- gluino pairs decaying to:

$$\tilde{g}\tilde{g} \rightarrow \tilde{b}_i b + \tilde{b}_j b, \quad \tilde{b}_i b + \tilde{t}_1 t, \quad \tilde{t}_1 t + \tilde{t}_1 t$$

⇒ good b tagging efficiency needed to reject these

- production of $\tilde{b}_i \tilde{b}_j^*$ and $\tilde{t}_2 \tilde{t}_2^*$ is order of magnitude smaller than the signal

- different final states within the signal may fake each other when top decays leptonically:

$$\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0 \rightarrow b \ell + E_{\text{miss}} \quad \text{and} \quad \tilde{t}_1 \rightarrow b \tilde{\chi}_1^+ \rightarrow b \ell + E_{\text{miss}}$$

⇒ can be combined together without spoiling the fit

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Conclusions

- if stops are too heavy for ILC we have to use maximum information from LHC
- proposed method can give useful constraints on parameters of stop sector
- additional precision measurement of gaugino/higgsino sector may be required from the linear collider
⇒ example of LHC-ILC interplay
- combination with CP-odd observables can resolve CP properties of top squarks
- more detailed experimental study needed to assess viability of this method

Additional slides

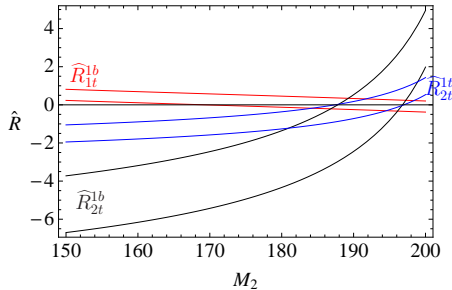
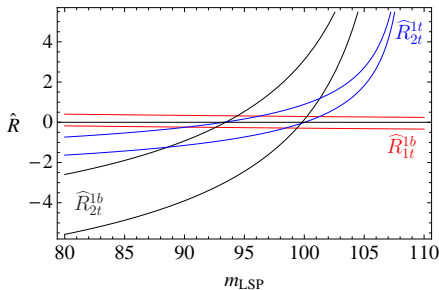
Possible final states

- for decay modes with t quark require top reconstruction
- neutralino decay modes include tau leptons
- number of events for integrated luminosity $\mathcal{L} = 100 \text{ fb}^{-1}$

decay mode	# events
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_2^0 + \bar{t} \tilde{\chi}_2^0 \rightarrow t \ell \bar{\ell} \tilde{\chi}_1^0 + \bar{t} \ell \bar{\ell} \tilde{\chi}_1^0 \rightarrow 4\ell \ 4j \ 2b + E_{\text{miss}}$	225
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_2^0 + \bar{t} \tilde{\chi}_1^0 \rightarrow t \ell \bar{\ell} \tilde{\chi}_1^0 + \bar{t} \tilde{\chi}_1^0 \rightarrow 2\ell \ 4j \ 2b + E_{\text{miss}}$	1270
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_2^0 + b \tilde{\chi}_1^+ \rightarrow t \ell \bar{\ell} \tilde{\chi}_1^0 + b \bar{\ell} \nu_e \tilde{\chi}_1^0 \rightarrow 3\ell \ 2j \ 2b + E_{\text{miss}}$	6230
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_1^0 + \bar{t} \tilde{\chi}_1^0 \rightarrow 4j \ 2b + E_{\text{miss}}$	7100
$\tilde{t}_1 \tilde{t}_1^* \rightarrow t \tilde{\chi}_1^0 + b \tilde{\chi}_1^+ \rightarrow t \tilde{\chi}_1^0 + b \bar{\ell} \nu_e \tilde{\chi}_1^0 \rightarrow \ell \ 2j \ 2b + E_{\text{miss}}$	35000
$\tilde{t}_1 \tilde{t}_1^* \rightarrow \bar{b} \tilde{\chi}_1^- + b \tilde{\chi}_1^+ \rightarrow \bar{b} \bar{\ell} \nu_e \tilde{\chi}_1^0 + b \bar{\ell} \nu_e \tilde{\chi}_1^0 \rightarrow 2\ell \ 2b + E_{\text{miss}}$	170000

Dependence on gaugino parameters

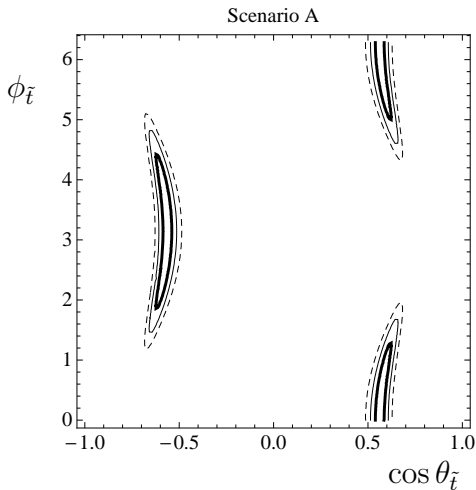
ratios of BRs show only moderate dependence on LSP mass
 (keeping $m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}$ fixed) and wino mass parameter M_2
 \Rightarrow no precise knowledge needed to get useful constraints



\Rightarrow stronger dependence only for decay to $\tilde{\chi}_2^0 t$ which is close to kinematical limit

Fit results for $\cos \theta_{\tilde{t}}$ and $\phi_{\tilde{t}}$

- 1000 events of stop production
- χ^2 fit to all 3 ratios
- error = statistical only
- the CP phase is unconstrained



Higgsino scenario

Features: bino LSP $\tilde{\chi}_1^0$; higgsino $\tilde{\chi}_1^+$, $\tilde{\chi}_2^0$ and $\tilde{\chi}_3^0$;

